

## Structural and Electronic Properties of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O Nanoclusters – a DFT Approach

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The realistic structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O were completely optimized using density functional theory approach. The different structures were optimized to study the structural stability, dipole moment, point symmetry, HOMO-LUMO gap, ionization potential, electron affinity and binding energy of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O. The electronic properties of clusters were discussed in terms of HOMO-LUMO gap, density of states, ionization potential and electron affinity. This information will provide an insight for the synthesis of nanomaterials with proper geometry which finds its potential importance in engineering applications.

**Keywords:** ionization potential, electron affinity, nanoclusters, HOMO-LUMO, binding energy.

### 1. INTRODUCTION

Oxygen combines with copper to form copper (I) oxide (Cu<sub>2</sub>O), copper (II) oxide (CuO) and copper dioxide (CuO<sub>2</sub>). These oxides of copper can bond with one or two electrons. Oxygen may form compound with metals by gaining two electrons, which may accept one electron from each of two copper atoms forming copper (I) oxide or it may accept two electrons from one atom, which forms copper (II) oxide. Cu<sub>2</sub>O is a p-type semiconductor also called as cuprous oxide; the potential application of Cu<sub>2</sub>O is in agriculture, used as an ingredient in many fungicides that protect from fungal diseases. It is also active component in antifouling paints [1], pigment in some types of glass [2], in ceramic glazes [3], as catalyst in chemical processes, photovoltaic and photocatalytic applications [4–7]. CuO is also known as cupric oxide; CuO is added to clay glazes as pigment [8] and used as abrasive for polishing lenses and optical components [9]. CuO<sub>2</sub> is one of the important compounds in superconducting lattice [10–12]. The preparation of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O in thin film form or as nanoparticles involves various methods such as thermal evaporation, RF sputtering, laser ablation, chemical vapour deposition, chemical bath deposition, sol-gel method, spray pyrolysis and electrodeposition methods [13–16]. The morphology such as nano needles, nanoflakes, nano rods and nanotube can be synthesized by proper controlling mechanism [17–19]. The nanoclusters can be formed by proper synthesis of the material in the plane oriented substrates or by capping the material through surfactant. The motivation of the present work is since CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O find its potential application; if the morphology and structure is properly tailored it will be suitable for engineering applications.

With this as motivation, survey was conducted in Scirus database and it was found that much work has not been carried out in tailoring the morphology of copper oxides. The density functional theory (DFT) approach is one method to study the structural and electronic properties which can be used to synthesis a new form of materials depending on their engineering applications. In this article an attempt has been made to study the properties of the realistic structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O nanoclusters.

### 2. COMPUTATIONAL METHODS

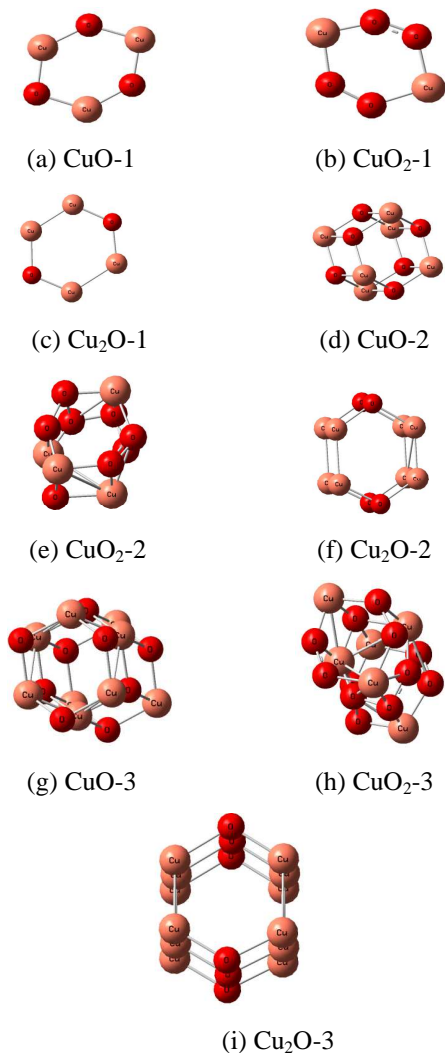
The possible structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters were completely optimized using NWChem package [20]. NWChem package is used to simulate complex biological and chemical structures for calculating in large scale. The conventional methods utilize Hartree-Fock calculation, which is carried out with a local basis set named as Fock build. In NWChem an algorithm known as Kohn-Sham matrix element is used to do the computation and energy convergence in DFT calculation. The electron correlation in DFT is taken into consideration through the exchange energy that arises from the antisymmetry of quantum mechanical wave function and dynamic correlation is used for the motion of the discrete electrons. DFT method involves the pseudo potential approximation to replace the complex effects of the bound electrons in the atom of the cluster that modifies the potential term of Schrödinger equation. The DFT method is exploited by using hybrid B3LYP exchange correlation for CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters with 6-31G basis set [21–24]. The atomic number of copper and oxygen are 29 and 8 respectively, 6-31G is a proper basis set to optimize the nanoclusters. In the present study, B3LYP/6-31G basis set is used throughout for all the structures. The energy convergence in the order of 10<sup>-5</sup> eV is achieved in the present work.

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### 3. RESULTS AND DISCUSSION

#### 3.1. Structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

Fig. 1 shows the various structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters. In the structure of CuO-1, the Cu atom and O atoms have hexagonal pattern like structure with Cu and O atoms attached alternatively, CuO<sub>2</sub>-1 structure has two Cu atoms and four O atoms in the form of hexagonal structure, in Cu<sub>2</sub>O-1 structure it has two O atoms attached to four Cu atoms forming a hexagonal structure.



**Fig 1.** Optimized structures of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

In the case CuO-2, CuO<sub>2</sub>-2 and Cu<sub>2</sub>O-2, they have two hexagonal layers one over the other with twelve atoms in total. In CuO-3, CuO<sub>2</sub>-3 and Cu<sub>2</sub>O-3 structures, the hexagonal layers are attached to the neighboring cluster forming a bee's hive like structures, considering all these types of realistic clusters, the energy, dipole moment and point symmetry are calculated and discussed.

Table 1 shows the calculated energy, dipole moment and point symmetry of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters. Among the structure of CuO-1, CuO<sub>2</sub>-1 and Cu<sub>2</sub>O-1 the energy for Cu<sub>2</sub>O-1 is  $-6711.371$  Hartrees which is more stable than the other structures, since in CuO<sub>2</sub>-1 which is rich in oxygen atoms is least stable which has the energy of  $-3590.941$  Hartrees. The dipole moment is maximum for CuO-1 due to asymmetry of the charge in the Cu and O

atoms in the cluster which is found to be 2.335 Debye. Cu<sub>2</sub>O-1 has the least dipole moment of 0.603 Debye, due to hexagonal structure in this type the point symmetry is C<sub>s</sub> for all the three clusters. In the case of CuO-2, CuO<sub>2</sub>-2 and Cu<sub>2</sub>O-2 clusters also the same trend is noticed as like of the previous clusters, since two layers of hexagonal structures are formed one over the other layer.

**Table 1.** Energy, dipole moment (DM) and point symmetry of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

Cluster	Energy (Hartrees)	DM (Debye)	Point symmetry
CuO-1	-5146.348	2.3356	C <sub>s</sub>
CuO <sub>2</sub> -1	-3580.941	0.8149	C <sub>s</sub>
Cu <sub>2</sub> O-1	-6711.371	0.6035	C <sub>s</sub>
CuO-2	-10292.586	0.5059	C <sub>1</sub>
CuO <sub>2</sub> -2	-7159.896	3.1266	C <sub>1</sub>
Cu <sub>2</sub> O-2	-13420.906	0.5708	C <sub>1</sub>
CuO-3	-12006.457	3.2664	C <sub>s</sub>
CuO <sub>2</sub> -3	-10440.506	0.0045	C <sub>s</sub>
Cu <sub>2</sub> O-3	-13569.948	0.0003	C <sub>2v</sub>

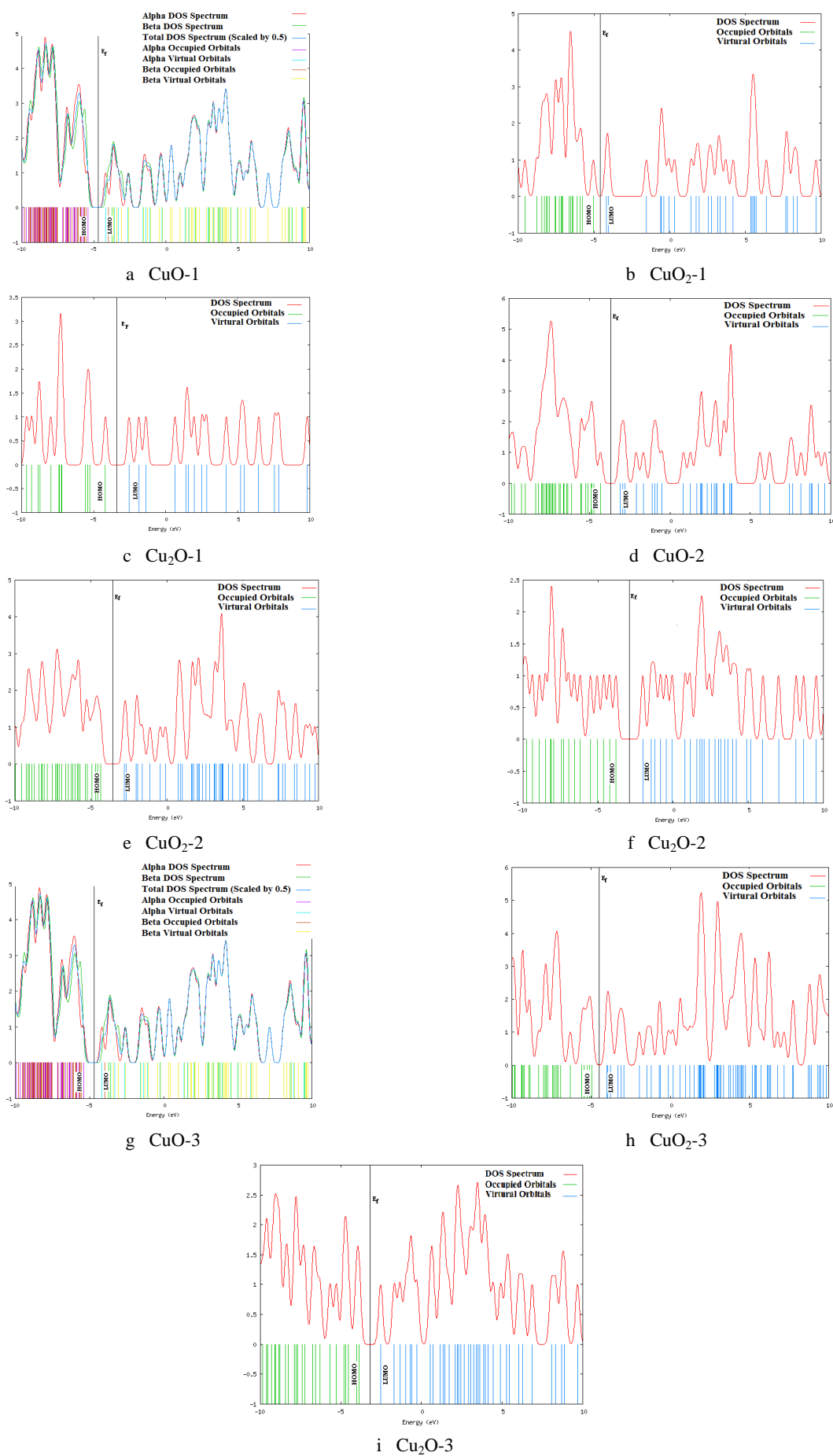
In this type, Cu<sub>2</sub>O cluster has the energy of  $-13420.90$  Hartrees which is more stable than the other two structures. The dipole moment is maximum for CuO<sub>2</sub> structure which is 3.126 Debye and least for CuO-2 which is 0.505 Debye, for all the cluster the point symmetry is C<sub>1</sub>. Interestingly, the energy increases for CuO-3, CuO<sub>2</sub>-3 and Cu<sub>2</sub>O-3 which has fourteen atoms in the cluster, Cu<sub>2</sub>O-3 has the energy of  $-13567.948$  Hartrees which is stable, CuO<sub>2</sub>-3 has the energy of  $-10440.506$  Hartrees which is least stable. The dipole moment is maximum for CuO-3 which is calculated to be 3.2664 Debye due to asymmetry in the structure. Both CuO<sub>2</sub>-3 and Cu<sub>2</sub>O-3 has low value of dipole moment which is 0.0045 and 0.0003 Debye respectively. The point symmetry for CuO-3 and CuO<sub>2</sub>-3 is C<sub>s</sub> and for Cu<sub>2</sub>O-3 is C<sub>2v</sub> which represents the asymmetry in the arrangement of atoms in the clusters. Comparing the energies of different clusters it is inferred that increase in the number of atoms in the cluster leads to the stability of the cluster.

#### 3.2. HOMO-LUMO gap and density of states of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

HOMO-LUMO gap of different clusters provides the insight for the electronic properties of clusters. Table 2 shows the energy gap between the HOMO-LUMO levels of different clusters. From the table it is seen that the gap of Cu<sub>2</sub>O-1, Cu<sub>2</sub>O-2 and Cu<sub>2</sub>O-3 are 0.86, 1.21 and 0.59 eV respectively, this clearly indicate the metallic nature of the cluster than the other two type of clusters namely CuO and CuO<sub>2</sub>.

Clearly it is also concluded that CuO<sub>2</sub>-1, CuO<sub>2</sub>-2 and CuO<sub>2</sub>-3 have a gap of 1.64, 1.79 and 1.73 eV respectively, due to rich oxygen atoms in these clusters the energy gap is more which match well with the experimental results [25].

In a particular cluster, which is having high value of gap, requires more energy to lift the electrons from the HOMO level to LUMO level. In contrast, the cluster which has low value of gap requires less energy to move the electron from HOMO to LUMO level. From this it is seen in these clusters Cu<sub>2</sub>O cluster have low gap which involves



**Fig. 2.** DOS Spectrum and HOMO-LUMO gap of CuO, Cu<sub>2</sub>O and Cu<sub>2</sub>O clusters

low energy to move the electron from the clusters, CuO<sub>2</sub> requires more energy to lift the electron and CuO clusters have moderate energy gaps. Since lower energy gap materials are highly reactive in chemical reactions and with catalyst, Cu<sub>2</sub>O-3 is highly reactive due to its lower energy gap. CuO-1 has the high value of band gap as 2.83 eV, which will not take part actively in chemical reactions.

**Table 2.** HOMO-LUMO gap of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

Clusters	HOMO(eV)	LUMO(eV)	Eg(eV)
CuO-1	-5.83	-3.00	2.83
CuO <sub>2</sub> -1	-4.18	-2.54	1.64
Cu <sub>2</sub> O-1	-5.04	-4.18	0.86
CuO-2	-4.31	-3.10	1.21
CuO <sub>2</sub> -2	-3.82	-2.03	1.79
Cu <sub>2</sub> O-2	-4.31	-3.10	1.21
CuO-3	-4.82	-3.29	1.53
CuO <sub>2</sub> -3	-3.85	-2.12	1.73
Cu <sub>2</sub> O-3	-5.22	-4.63	0.59

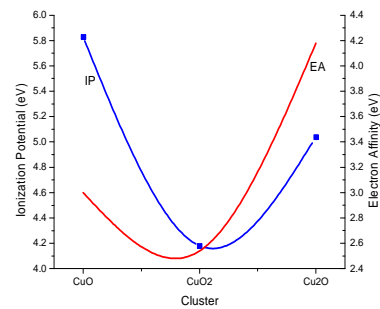
The density of states (DOS) spectrum provides perception about the presence of the charge in the particular energy interval. In the case of CuO-1 due to the equal number of copper and oxygen atoms present in the cluster leads to the overlapping of orbitals. The electron with spin up will give rise to alpha orbital and electrons with spin down will give rise to beta orbital. The alpha and beta orbital are seen only in the CuO-1 and CuO-3, whereas in the CuO-2 the presence of the atoms of copper and oxygen one over the other layer balance the spin of the electrons and no alpha and beta orbital are noticed in the case of CuO-2 cluster. Even in the DOS spectrum of CuO-1 the charges are far away from the Fermi level ( $E_F$ ) which is noticed in the occupied orbitals. More number of peaks is observed in the virtual orbitals. In CuO<sub>2</sub> cluster the charges are localized near the Fermi level and wide gap is noticed between the adjacent levels in the virtual orbitals.

In CuO-2 cluster only some peak are seen in the occupied and virtual orbitals. In CuO<sub>2</sub>-2 more broad density of charges are seen over wide energy range. Looking at the spectrum of Cu<sub>2</sub>O-2 more number of periodic peaks is seen throughout the occupied and virtual orbitals again confirming more metallic nature. Analyzing the spectrum of CuO-3 the presence of more layers leads to broad peaks in occupied and virtual orbitals. In CuO<sub>2</sub>-2 spectrum, maximum peak heights are noticed, which refer to the delocalization of charges in the virtual orbitals. Interesting observation in the case of Cu<sub>2</sub>O-3 cluster is maximum peak heights are noticed throughout the occupied and virtual orbitals again confirms narrow band gap. The DOS provides the insight towards the density of the charges in the occupied and virtual orbitals. Figure 2, a-i, shows the DOS spectrum and HOMO-LUMO gap of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters respectively.

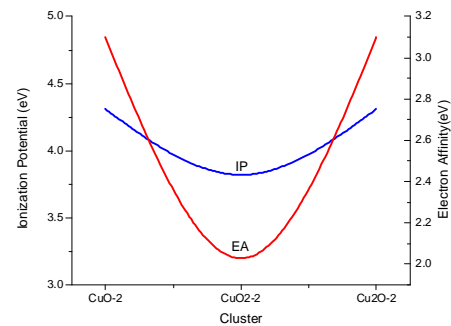
### 3.3. Ionization potential and electron affinity of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

Fig. 3, Fig. 4 and Fig. 5 shows the ionization potential (IP) and electron affinities (EA) of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters. The ionization potential refers to the energy

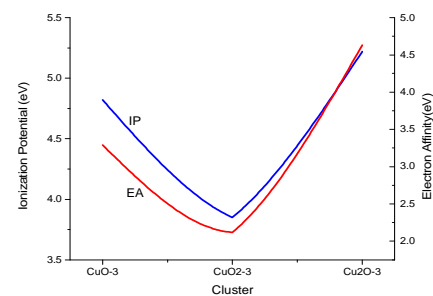
required to separate the electron from the cluster. Among all the clusters a high value of IP is noticed for CuO-1, Cu<sub>2</sub>O-1 and Cu<sub>2</sub>O-3 which has the IP of 5.83, 5.04 and 5.22 eV respectively this infers that these clusters will not actively take part in the chemical reactions. The high value of EA denotes the change in energy when an electron is added to the cluster, among all the clusters Cu<sub>2</sub>O clusters found to have high value of EA due to more number of copper atoms in this clusters which shows slight metallic type of behaviour, Cu<sub>2</sub>O clusters are more suitable for the chemical sensor applications since the change in energy takes place rapidly in these clusters [26, 27]. The EA of different nanoclusters are also in agreement with the reported results of Cu<sub>n</sub>O<sub>n</sub> for n = (1 – 8) clusters [28] and Cu<sub>2</sub>O<sub>x</sub> for x = (1 – 4) [29].



**Fig. 3.** Variation of ionization potential (IP) and electron affinity (EA) of CuO-1, CuO<sub>2</sub>-1 and Cu<sub>2</sub>O-1 clusters



**Fig. 4.** Variation of ionization potential (IP) and electron affinity (EA) of CuO-2, CuO<sub>2</sub>-2 and Cu<sub>2</sub>O-2 clusters



**Fig. 5.** Variation of ionization potential (IP) and electron affinity (EA) of CuO-3, CuO<sub>2</sub>-3 and Cu<sub>2</sub>O-3 clusters

### 3.4. Binding energies of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

The binding energy (BE) per atom of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters for different structures are calculated using the following relation [30]:

$$BE = [(nE(\text{Cu}) + mE(\text{O}) - E(\text{Cu}_n\text{O}_m))/(n + m)], \quad (1)$$

where  $E(\text{Cu})$  is the energy of Cu atom,  $E(\text{O})$  is the energy of O atom,  $n$  and  $m$  are number of Cu and O atoms respectively. The calculated binding energies for different clusters are tabulated in Table 3. Among all the clusters CuO-1, CuO<sub>2</sub>-1, Cu<sub>2</sub>O-1 and CuO-2 has the BE of 4.38, 3.52, 3.50 and 4.13 eV respectively. The high value of BE infers that these clusters are stable; since all the clusters are having hexagonal structure, this results in high value of BE [31].

**Table 3.** Binding energies of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O clusters

Clusters	BE (eV)
CuO-1	4.38
CuO <sub>2</sub> -1	3.52
Cu <sub>2</sub> O-1	3.50
CuO-2	4.13
CuO <sub>2</sub> -2	1.95
Cu <sub>2</sub> O-2	1.31
CuO-3	1.10
CuO <sub>2</sub> -3	0.75
Cu <sub>2</sub> O-3	2.25

#### 4. CONCLUSION

The realistic nanoclusters of CuO, CuO<sub>2</sub> and Cu<sub>2</sub>O are completely optimized using B3LYP/6-31G basis set. The energy, dipole moment and point symmetry of geometrically optimized nanoclusters are studied and discussed. The dipole moment arises due to the uneven charge distribution in the atoms of the different clusters. The stability of the clusters is discussed in terms of calculated energy, binding energy. The binding energies of CuO-1 and CuO<sub>2</sub>-1, Cu<sub>2</sub>O-1 and CuO-2 are found to be high among all the clusters. The high value of HOMO-LUMO gap is discussed which gives the information about the transition of electrons. DOS spectrum provides the perception about the presence of charge in various energy intervals. The high value of IP is noticed for CuO-1, Cu<sub>2</sub>O-1 and Cu<sub>2</sub>O-3 clusters. Cu<sub>2</sub>O clusters have high value of EA which is due to the metallic nature of the cluster. The reported information will provide an insight for the experimentalist to synthesis new material which has its potential importance in the industrial applications.

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