

## Predicting Thin Film Stoichiometry in V-O<sub>2</sub> Reactive Sputtering

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The electrical, optical and mechanical properties of compound oxides film depend strongly on the composition of the film, especially for vanadium oxide thin films, since the vanadium-oxygen phase diagram includes mixed valence oxides with two or more oxidation states. Therefore, it is interesting to predict the film stoichiometry in VO<sub>x</sub> films. However, it has not, to any great extent yet, been possible to predict the composition of vanadium oxides films. In this article, we present a model that enables us to predict film composition of vanadium oxides prepared by reactive sputtering. Based on this model, the fraction ratio of V, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub> in the substrate surface as a function of oxygen flow is investigated. It is concluded that the presented theoretical model for the involved reactions and composition of VO<sub>x</sub> thin film during reactive sputtering process is in qualitative agreement with the XPS results from experiment and can be used to find optimum processing conditions for deposition of films of a desired composition.

*Keywords:* vanadium oxide, film composition, reactive sputtering, theoretical model.

### 1. INTRODUCTION

As one of the fascinating material with excellent physical and chemical properties, vanadium oxide thin films have been studied extensively [1, 2]. VO<sub>x</sub> films with mixture phases can be tailored to meet the demand of reasonable resistivity and relatively high temperature coefficient of resistivity (TCR), these materials have become the mainstream technology in the fast booming uncooled infrared image market. Therefore, research on the preparation techniques of VO<sub>x</sub> thin films, has greatly been stimulated. However, the vanadium-oxygen system is a very complex compound system, because vanadium exhibits +2, +3, +4 and +5 valent states, a large number of vanadium oxides, such as VO, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub>, V<sub>2</sub>O<sub>5</sub>, V<sub>2n</sub>O<sub>5n-2</sub> and V<sub>n</sub>O<sub>2n-1</sub> exist in the VO<sub>x</sub> films. Vanadium oxides show different electronic behaviour depending on their valence configuration. The electronic and optical performance of vanadium oxide is relative to the structure of the thin films. Moreover, the reproducibility and stability of electrical properties of vanadium oxide films are dependent on the ratio of vanadium and oxygen in the film. Hence, understanding of the influence of process parameters on the film composition and microstructure is necessary. In this case, how to predict the film stoichiometry and then adjust the optical, electrical properties of the VO<sub>x</sub> films for particular applications became a challenge.

Vanadium oxide thin films have been widely prepared by reactive magnetron sputtering method [3]. Theoretical modelling can be used as a tool to increase the understanding of this complex process. The mechanism of reactive sputtering was reasonably well described by the Berg model [4, 5], and recently the extensions to this model have been published [6–11]. Theoretical analysis of

compounds with mixed vanadium oxide thin films have been published previously [12], however, only suboxide VO on the target was taken into consideration in the modeling and the corresponding experimental results was not given. In this paper, we assumed metal vanadium and three oxides of V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub> was formed on both target and substrate during V–O<sub>2</sub> reactive sputtering. Based on this assumption, more complex processes between substrate and target such as different atoms sputtered from target which dropped on substrate are involved in this model. The details are shown in the following model section. In the experimental part, we report vanadium oxide thin films deposited by magnetron sputtering method with different oxygen flows and investigate the changing fraction of V, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub> with respect to the oxygen flow using XPS analysis.

### 2. MODEL

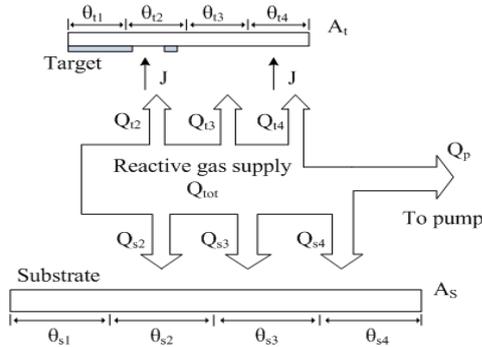
A model describing the dynamic behaviour of the reactive sputtering process for vanadium oxide has been presented previously [12]. That model takes into account vanadium metal on the target and VO<sub>x</sub> of two different valence oxides (VO and V<sub>2</sub>O<sub>5</sub>) on the substrate. However, from the results of XPS measurement taken on the VO<sub>x</sub> samples (will be seen in the experimental part), V, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub> have been observed. The starting point of Berg's model is aimed at defining the processing conditions as correct as possible. Therefore, a new model is developed which accounts for the existence of the four states of vanadium oxides based on the experimental results. The suggested model is a further development of previously presented models.

Analogous to the earlier models, the targets are assumed to be partially covered with the compound and metal materials. The total supply rate of the reactive gas (oxygen) is denoted as  $Q_{tot}$ . In order to simulate this more

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efficiently, we made some additional assumptions. On one hand, the same conditions exist at the receiving area where all sputtered material is assumed to be uniformly collected.

Different from the previous model, the target surface must be divided into four parts (see Fig. 1). Here  $\theta_{t1}$  is denoted as the fractional area of the target surface that consists of unreacted metal vanadium. The  $\theta_{t2}$ ,  $\theta_{t3}$ ,  $\theta_{t4}$  fraction would be assumed to be covered by  $V_2O_3$ ,  $VO_2$  and  $V_2O_5$ , respectively.  $\theta_{s1}$  is the fractional area of the substrate surface that consists of unreacted metal vanadium and the  $\theta_{s2}$ ,  $\theta_{s3}$ ,  $\theta_{s4}$  fractions are covered by  $V_2O_3$ ,  $VO_2$  and  $V_2O_5$ , respectively.



**Fig. 1.** Schematic of a simple reactive- sputtering system

## 2.1. Conditions at the target surface

Compare with the previous modelling, more simplifications must be made to keep the complexity down without losing contact with reality. For one thing, it is assumed that the gettering of reactive gas onto metal contributes to form a suboxide  $V_2O_3$  on the substrate, increasing  $\theta_{s2}$  and decreasing  $\theta_{s1}$ . Further attachment (by oxygen) onto this suboxide  $V_2O_3$  contributes to form the  $VO_2$ , thus increasing  $\theta_{s3}$ , also decreasing  $\theta_{s2}$ . The superoxide  $V_2O_5$  is formed by the reaction of reactive gas and  $VO_2$ . For the other thing, additional process happened on the substrate needs to be considered. As for the metal vanadium sputtered from the target, when the metal comes from the fraction of  $\theta_{t1}$  placed on the substrate surface which previously consisted of  $VO_x$  ( $V_2O_3$ ,  $VO_2$  and  $V_2O_5$ ), that the fraction of  $\theta_{s1}$  will increase and the fraction of  $(1-\theta_{s1})$  will decrease. Furthermore, when the  $VO_x$  particle sputtered from target placed on the substrate, which previously consisted of  $VO_i$  ( $i! = x$ ), then the corresponding fraction of  $\theta_{si}$  will decrease and the fraction of  $VO_x$  will increase. The fraction of flux  $\frac{J}{q}Y_{ii}\theta_{ii}A_t$  deposited onto the

fraction  $\theta_{si}$  of the collecting area  $A_s$  will not influence the value of  $\theta_{s1}$ . Adding elemental non-reacted target atoms to an area that already consist of non-reacted atoms does not change  $\theta_{s1}$ .

By making the above-mentioned new assumptions in combination with the simplifications presented earlier, the balance equations for the conditions on the target should be rewritten as the following equation:

$$\frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t = 2\alpha_{t1}FA_t\theta_{t1}/l_2, \quad (1)$$

here  $J$  is the ion-current density,  $q$  is the elementary electronic charge.  $Y_{t2}$ ,  $Y_{t3}$ ,  $Y_{t4}$  represent the sputtering yield

of the  $V_2O_3$ ,  $VO_2$  and  $V_2O_5$ .  $\alpha_{t1}$  is the probability (sticking coefficient) for a oxygen molecule to react with a vanadium atom that comes from the  $\theta_{t1}$  fraction of the target,  $A_t$  is the effective target.  $l_2$  is the stoichiometry of the  $V_2O_3$  taken into consider in this model,  $F$  represents neutral reactive molecules/ (unit area and time).

Eq. (1) determines the balance of the fraction of vanadium atoms ( $\theta_{t1}$ ) on the target. For simplicity, the sputtered material from the surface fraction  $\frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t$  is assumed to be sputtered as molecules, irrespective of whether the material is ejected in atomic or molecular form. The only way sputtered compound molecules may be replaced is by reactions between neutral reactive gas molecules and the elemental non-reacted vanadium atoms:

$$2\alpha_{t1}FA_t\theta_{t1}/l_2 = \frac{J}{q}Y_{t2}\theta_{t2}A_t + 2\alpha_{t2}FA_t\theta_{t2}/(l_3 - l_2), \quad (2)$$

here,  $\alpha_{t2}$  is the sticking coefficient for the oxygen molecule to react with  $V_2O_3$  from the fraction  $\theta_{t2}$  of the target,  $l_3$  is the stoichiometry of the  $VO_2$ .

Moreover, Eq. (2) determines the balance of the fraction of  $\theta_{t2}$  on the target. The reaction between elemental target atoms and the reactive gas which takes place on the compound fraction  $\theta_{t1}$  will contribute to an increase in the value of  $\theta_{t2}$ . However, the compound  $V_2O_3$  are sputtered from the surface fraction  $\theta_{t2}$  that will decrease the fraction of  $\theta_{t2}$ . Besides, attaching the reactive gas to  $V_2O_3$  will contribute to a decrease in  $\theta_{t2}$ :

$$2\alpha_{t2}FA_t\theta_{t2}/(l_3 - l_2) = \frac{J}{q}Y_{t3}\theta_{t3}A_t + 2\alpha_{t3}FA_t\theta_{t3}/(l_4 - l_3); \quad (3)$$

$$2\alpha_{t3}FA_t\theta_{t3}/(l_4 - l_3) = \frac{J}{q}Y_{t4}\theta_{t4}A_t, \quad (4)$$

here,  $\alpha_{t3}$  is the probability (sticking coefficient) for the oxygen molecule to react with  $VO_2$  from the fraction  $\theta_{t3}$  of the target,  $l_4$  is the stoichiometry of the  $V_2O_5$ .

Similar to Eq. (2), Eq. (3) and Eq. (4) determine the balance of the fraction of  $\theta_{t3}$  and  $\theta_{t4}$  respectively:

$$\theta_{t1} + \theta_{t2} + \theta_{t3} + \theta_{t4} = 1. \quad (5)$$

The expressions for  $\theta_{t1}$ ,  $\theta_{t2}$ ,  $\theta_{t3}$ ,  $\theta_{t4}$  can be obtained by solving Eqs. (2)–(5).

## 2.2. Conditions at the substrate surface

At steady state, the contributions supporting an increase in  $\theta_{si}$  must be identical to the contributions that support a decrease in  $\theta_{si}$ . This leads to the following balance equations (Eqs. (6) through (10)) for the collecting area  $A_s$ .

Eq. (6) determines the balance of the fraction of  $\theta_{s1}$  on the substrate. The fraction of flux  $\frac{J}{q}Y_{t1}\theta_{t1}A_t$  deposited onto the fraction  $(1-\theta_{s1})$  will increase the value of  $\theta_{s1}$ . The fraction of flux  $\frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t$  deposited onto the fraction  $(\theta_{s1})$  will contribute to a decrease in  $\theta_{s1}$ . The number of molecules which convert into  $V_2O_3$  by oxygen is denoted by  $2\alpha_{s1}FA_s\theta_{s1}/l_2$ . The reaction between elemental non-reacted atoms and reactive gas will decrease the value of  $\theta_{s1}$ :

$$\frac{J}{q}Y_{t1}\theta_{t1}A_t(1-\theta_{s1}) = \quad (6)$$

$$= \left(\frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t\right)\theta_{s1} + 2\alpha_{s1}FA_s\theta_{s1}/l_2$$

here  $\alpha_{s1}$  is the sticking coefficient for the oxygen molecule to react with vanadium atom on the substrate.

$$\begin{aligned} & \frac{J}{q}Y_{t2}\theta_{t2}A_t(1-\theta_{s2}) + 2\alpha_{s1}FA_s\theta_{s1}/l_2 = \\ & = \left(\frac{J}{q}Y_{t1}\theta_{t1}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t\right)\theta_{s2} + \quad (7) \\ & + 2\alpha_{s2}FA_s\theta_{s2}/(l_3-l_2) \end{aligned}$$

$\alpha_{s2}$  is the sticking coefficient for the oxygen molecule to react with  $V_2O_3$  on the substrate.

Eq. (7) determines the balance of the fraction of  $\theta_{s2}$  on the substrate. The fraction of flux  $\frac{J}{q}Y_{t2}\theta_{t2}A_t$  deposited

onto the fraction  $(1-\theta_{s2})$  will increase the value of  $\theta_{s2}$ . Besides, the reaction between elemental non-reacted atoms and reactive gas will increase the value of  $\theta_{s2}$ . However, the fraction of flux  $\frac{J}{q}Y_{t1}\theta_{t1}A_t + \frac{J}{q}Y_{t3}\theta_{t3}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t$  deposited onto the fraction  $(\theta_{s2})$  will contribute to a decrease in  $\theta_{s2}$ . The flux  $2\alpha_{s2}FA_s\theta_{s2}/(l_3-l_2)$  consumed by the reaction between compound  $V_2O_3$  and reactive gas will decrease the value of  $\theta_{s2}$ :

$$\begin{aligned} & \frac{J}{q}Y_{t3}\theta_{t3}A_t(1-\theta_{s3}) + 2\alpha_{s2}FA_s\theta_{s2}/(l_3-l_2) = \\ & = \left(\frac{J}{q}Y_{t1}\theta_{t1}A_t + \frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t\right)\theta_{s3} + \quad (8) \\ & + 2\alpha_{s3}FA_s\theta_{s3}/(l_4-l_3) \end{aligned}$$

$\alpha_{s3}$  is the sticking coefficient for the oxygen molecule to react with  $VO_2$  on the substrate.

Eq. (8) determines the balance of the fraction of  $\theta_{s3}$  on the substrate. The fraction of flux  $\frac{J}{q}Y_{t3}\theta_{t3}A_t$  deposited

onto the fraction  $(1-\theta_{s3})$  will increase the value of  $\theta_{s3}$ . Besides, the reaction between compound  $V_2O_3$  and reactive gas will increase the value of  $\theta_{s3}$ . However, the fraction of flux  $\left(\frac{J}{q}Y_{t1}\theta_{t1}A_t + \frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t\right)\theta_{s3}$  deposited onto the fraction  $(\theta_{s2})$  will contribute to a decrease in  $\theta_{s2}$ . Moreover, the flux  $2\alpha_{s3}FA_s\theta_{s3}/(l_4-l_3)$  consumed by the reaction between compound  $VO_2$  and reactive gas will decrease the value of  $\theta_{s3}$ .

Similar to the above discussion, a steady-state equation for the fraction of  $V_2O_5$  on the substrate may therefore be defined as:

$$\begin{aligned} & \frac{J}{q}Y_{t4}\theta_{t4}A_t(1-\theta_{s4}) + 2\alpha_{s3}FA_s\theta_{s3}/(l_4-l_3) = \\ & = \left(\frac{J}{q}Y_{t1}\theta_{t1}A_t + \frac{J}{q}Y_{t2}\theta_{t2}A_t + \frac{J}{q}Y_{t4}\theta_{t4}A_t\right)\theta_{s4} \quad (9) \end{aligned}$$

Finally, the sum of fractions  $(\theta_{s1}, \theta_{s2}, \theta_{s3}, \theta_{s4})$  is equal to 1:

$$\theta_{s1} + \theta_{s2} + \theta_{s3} + \theta_{s4} = 1. \quad (10)$$

### 2.3. Gettering of the reactive gas

Compound formation by reaction between reactive gas molecules and elemental non-reacted atoms, compound  $V_2O_3$ , compound  $VO_2$  at the target will consume reactive gas molecules  $Q_{t1}$ ,  $Q_{t2}$ ,  $Q_{t3}$  reactively. Thus, the consumption (number of oxygen molecules per unit time) at the target  $Q_t$  can be obtained from Eq. (11):

$$\begin{aligned} Q_{t1} &= 2\alpha_{t1}FA_t\theta_{t1}/l_2; \\ Q_{t2} &= 2\alpha_{t2}FA_t\theta_{t2}/(l_3-l_2); \\ Q_{t3} &= 2\alpha_{t3}FA_t\theta_{t3}/(l_4-l_3); \\ Q_t &= Q_{t1} + Q_{t2} + Q_{t3}. \end{aligned} \quad (11)$$

While the consumption  $Q_s$  at the collecting area  $A_s$  can be expressed by Eq. (12):

$$\begin{aligned} Q_{s1} &= 2\alpha_{s1}FA_s\theta_{s1}/l_2; \\ Q_{s2} &= 2\alpha_{s2}FA_s\theta_{s2}/(l_3-l_2); \\ Q_{s3} &= 2\alpha_{s3}FA_s\theta_{s3}/(l_4-l_3); \\ Q_s &= Q_{s1} + Q_{s2} + Q_{s3}. \end{aligned} \quad (12)$$

Here,  $Q_{s1}$  is reactive gas molecules consumed by reactive gas oxygen molecules and non-reacted vanadium atoms at collecting area.  $Q_{s2}$  is reactive gas molecules consumed by oxygen and  $V_2O_3$  compound. The other part  $Q_{s3}$  is reactive gas molecules consumed by oxygen and  $VO_2$  compound.

The remaining part  $Q_p$  of the reactive gas will escape from the processing chamber through the pumping system:

$$Q_p = \frac{PN_a}{R_r T} S, \quad (13)$$

here,  $P$  is the partial pressure of oxygen,  $N_a$  is Avogadro constant,  $R_r$  is general gas constant,  $T$  is the temperature,  $S$  is the pumping speed.

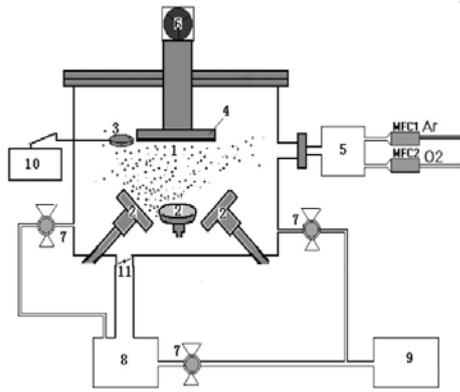
Eqs. (1) through (5) describe the conditions at the target, in conjunction with Eqs. (6) through (10), make up a set of equations that can be easily solved by a computer.

The total supply rate of the reactive gas is denoted  $Q_{tot}$ :

$$Q_{tot} = Q_t + Q_s + Q_p. \quad (14)$$

### 3. EXPERIMENTAL

$VO_x$  thin films were deposited by DC reactive magnetron sputtering in a custom-built vacuum system, as shown in Fig. 2. A water cooled rectangle planar vanadium metal target, with the purity level of 99.99 %, was used in these experiments. The deposition chamber was evacuated to a base pressure of about  $1.0 \times 10^{-4}$  Pa by combining turbomolecular and rotary vane pumps. Argon and oxygen flow were controlled by using independent mass flow controllers, the argon flow was kept constant at 100 sccm and the oxygen flow was varied from 1.0 sccm to 6.0 sccm. Glass slides were used as substrates. Before the substrates were mounted on a substrate holder, they were ultrasonically cleaned in acetone, ethanol and de-ionized water for 20 min sequentially, and then dried by pure nitrogen stream. For all the experiments, two steps were applied: cleaning of the vanadium target surface by pre-sputtering of 15 min in a pure argon atmosphere, followed by reactive deposition of  $VO_x$  films for around 25 min. The substrate holder was rotated at 10 rpm to ensure uniformity of film deposition and there were no intentionally heating during experiment. So the deposition temperature is 300 K.

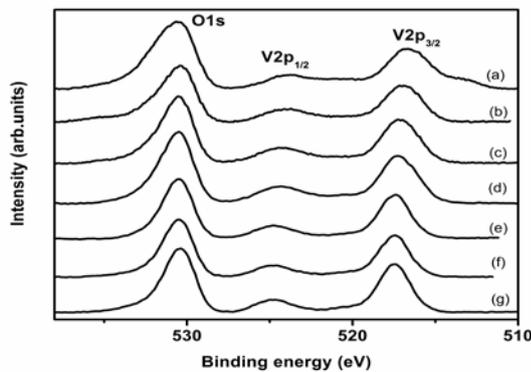


**Fig. 2.** Reactive sputter deposition system (1) substrate (2) magnetron sources (3) quartz microbalance (4) resistive heater (5) gas supply (6) rotating controller (7) small angle valves (8) turbo pump (9) rotary pump (10) frequency meter (11) slide valve

X-ray photoelectron spectroscopy (XPS) spectra were taken by using XSAM800 system (Kratos Ltd., Al K $\alpha$  X-ray source without monochromatization, the base pressure of the ultrahigh vacuum chamber was lower than  $3 \times 10^{-7}$  Pa, binding energies (BE) were determined using C1s peak at 284.8 eV as a reference, the resolution is 0.9 eV/ $10^4$  counts per second).

#### 4. RESULTS AND DISCUSSION

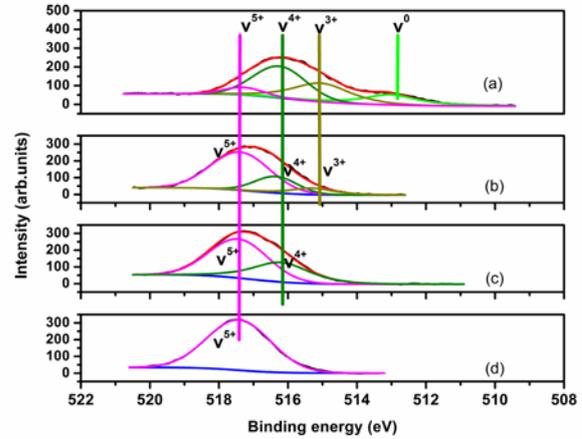
The influence of the oxygen flow rate on the stoichiometry of the deposited vanadium oxide was examined by the X-ray photoemission spectroscopy (XPS). To avoid surface effects, like contamination, the XPS spectra were taken in the depth of the samples after preliminary sputtering.



**Fig. 3.** XPS spectra of the V 2p and O 1s region of films. Oxygen flow is: a – 1 sccm; b – 3 sccm; c – 3.8 sccm; d – 4.2 sccm; e – 4.4 sccm; f – 4.6 sccm; g – 6 sccm

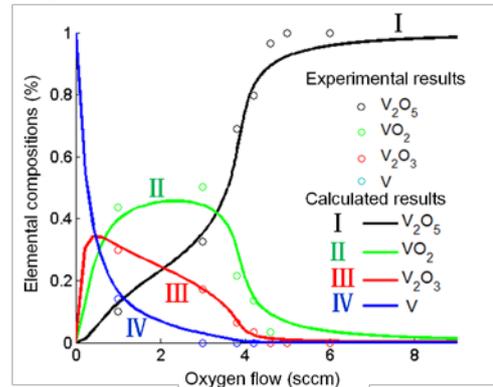
Fig. 3 shows the XP spectra of the O 1s and V 2p core level emission lines taken at different samples with varied oxygen flow. Spectra (a–g) show that the V 2p<sub>3/2</sub> and V 2p<sub>1/2</sub> lines become narrower and shift to higher binding energies with increasing oxygen flow, suggesting more vanadium fractions with higher oxidation states existed in the film. In order to analyze this process in more detail, the background corrected XPS spectra of the V 2p<sub>3/2</sub> lines was fitted with mixed Lorentzian-Gaussian [13] profiles after subtraction of a Shirley function [14–15] using software XPSpeak4.1. In Fig. 4, the lines in different colours centred at 512.6, 515.1, 516.2 and 517.2 eV show presence of

different components. Comparison of these values with the data found in the literature [16–20] allows attributing these components to V, V<sup>3+</sup>, V<sup>4+</sup>, and V<sup>5+</sup> oxidation states of vanadium, respectively.



**Fig. 4.** V 2p<sub>3/2</sub> lines of vanadium oxides film taken at different samples with different oxygen flow. Oxygen flow is: a – 1 sccm; b – 4.2 sccm; c – 4.4 sccm; d – 6 sccm

When the oxygen flow is fairly low (spectrum (a)), all the four species state was found. With increasing oxygen flow (spectrum (b)), V<sup>0</sup> species disappear gradually which is due to the higher oxygen concentration. When oxygen flow is increased to around 4.4 sccm, the intensity of V<sup>3+</sup> species is removed. At high oxygen flow (spectrum (d)), only V<sup>5+</sup> species are existed.



**Fig. 5.** Experimental results and simulations of the elemental compositions (V, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub>) vs. different oxygen flow

It is possible to combine Eqs. (1) through (14) and solve all the fractions of target and substrate vs. reactive gas flow  $Q_{tot}$ . From the simulation results obtained, the substrate surface coverage has been estimated. The elemental compositions versus oxygen flows from these experiments and simulations are shown in Fig. 5. It is seen that  $\theta_{s1}$ , corresponding to the fractional area of the substrate consisting of metal vanadium, decreases most rapidly for low reactive gas flows, but decreases asymptotically to zero for high flows. In the region up to 3.5 sccm, the fraction of  $\theta_{s4}$  is higher than  $\theta_{s3}$  and  $\theta_{s1}$  reaches almost zero. Furthermore, with the continued increasing amount of oxygen,  $\theta_{s4}$  increases asymptotically to one. Meanwhile, the fraction of metal V, V<sub>2</sub>O<sub>3</sub> and VO<sub>2</sub> is reduced and eventually disappeared. It is seen that the trends in the experiments are adequately

described by the simulations. There are several reasons to explain these curves. For zero flow of oxygen, the target is to some extent oxidized and the rest is metallic, while at higher flows of oxygen, target is essentially oxidized. After the 3.5 sccm point, the amount of O<sub>2</sub> consumed to VO<sub>2</sub> surpassed the amount of O<sub>2</sub> gettered by deposited V and V<sub>2</sub>O<sub>3</sub>, resulting in a drastic increase in the fraction of  $\theta_{s4}$ . It should also be noted that the content of V<sub>2</sub>O<sub>3</sub> decreases from around 35 % to approximately 10 % in the region from 0.6 sccm to 3.8 sccm while the content of VO<sub>2</sub> is somewhat increased from 35 % to 42 %. This means that the films contain significantly more VO<sub>2</sub> than V<sub>2</sub>O<sub>3</sub>. This is a consequence of the higher reactivity of V<sub>2</sub>O<sub>3</sub> than V with oxygen. However, even though the trends are correctly reproduced in the simulations, there are discrepancies between the experiments and simulations. The content of VO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub> for experiments is somewhat higher while the content of metal V is somewhat lower than that of simulations. There are several factors contributing to the discrepancies in simulation results with respect to the experimental results. Unfortunately, it is not possible to sort out the effects in order of their impact. It assumed in the simulations that the content of metal V was 100 % for zero flow of oxygen, but the target is usually to some extent oxidized initially. Moreover, there might be pressure gradients in the system that is not considered in the simulations. Another error is from XPS analysis.

## 5. CONCLUSION

A kinetic model of reactive sputtering is proposed to modify Berg's model by taking into account the four species state of V, V<sub>2</sub>O<sub>3</sub>, VO<sub>2</sub>, and V<sub>2</sub>O<sub>5</sub> in the vanadium oxides film. The fraction of compound on the substrate has been investigated as a function of reactive gas flow during the reactive sputtering of multicomponent thin film. From the results of simulation, substrate surface coverage has been estimated. Vanadium oxide films have been deposited by reactive magnetron sputtering using a constant current and varying the oxygen flow. Film compositions obtained from the XPS analysis were compared to the composition obtained from simulations and the agreement is satisfactory. The results from modeling are compared with the corresponding experimental results. The model can be used to find optimum processing conditions for deposition of films of a desired VO<sub>x</sub> composition.

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## APPENDIX A

The following simulation parameters were used in the work:  $\alpha_{t1} = 0.95$ ,  $\alpha_{t2} = 0.95$ ,  $\alpha_{t3} = 0.95$ ,  $\alpha_{s1} = 1$ ,  $\alpha_{s2} = 1$ ,  $\alpha_{s3} = 1$ ,  $Y_{t1} = 0.6$ ,  $Y_{t2} = 0.3$ ,  $Y_{t3} = 0.2$ ,  $Y_{t4} = 0.2$ . Target area  $A_t = 260 \text{ cm}^2$ , gas temperature  $T = 300 \text{ K}$ , pumping speed  $S = 0.2 \text{ m}^3/\text{s}$ .

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