# DFT Calculation on the Electronic Structure and Optical Properties of In<sub>x</sub>Ga<sub>1-x</sub>N Alloy Semiconductors

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Using the density functional theory (DFT) of the first principle and Generalized gradient approximation method, the electronic structures and optical properties of the  $In_xGa_{1-x}N$  crystals with different x (x = 0.25, 0.5, 0.75, 1) have been calculated in this paper. The influence of the electronic structure on the properties has been analyzed. Then the influence of doping quantity on the characteristics has been summarized, which also indicates the trend of complex dielectric function, absorption spectrum and transitivity. With the increase of x, the computational result shows that the optical band gap (i.e.Eg) of the  $In_xGa_{1-x}N$  crystal tends to be narrow, then the absorption spectrum shifts to the low-energy direction. And the Fermi energy slightly moves to the bottom of conduction band which would cause the growth of conductivity by increasing x. In a word, the  $In_xGa_{1-x}N$  compound can be achieved theoretically the adjustable Eg and photoelectric performance with x, which will be used in making various optoelectronic devices including solar cell and sensors. *Keywords:*  $In_xGa_{1-x}N$  crystal, electronic structure, optoelectronic property, density functional theory.

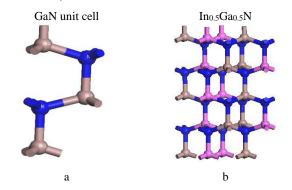
# **1. INTRODUCTION**

Due to the rapid development of microelectronics technology, InN-based semiconductor materials such as binary InN or ternary InGaN crystals that belong to directgap semiconductors have received much attention. They become one hotspot of the third generation semiconductors, which have the favorable electronic and optical properties including its high carrier mobility, higher breakdown voltage, high speed and a considerable range of emissions in the visible spectrum [1]. They can be also applied to many devices such as power electronics, sensors, high-efficiency solar cells, light emitting diodes at relatively long-visible wavelengths (LVW) and high electron mobility transistors (HEMTs) [1-3].

Many scholars have studied InGaN. Firstly, they focused on that InN and In<sub>x</sub>Ga<sub>1-x</sub>N materials can be prepared in different growth technologies with different In and Ga raw materials [4, 5]. Paying attention to study on InGaN quantum well [6]and growth of n - polar InGaN alloy films on high quality n-polar GaN templates [7]. Secondly, the band gap of InGaN alloy has been calculated [8]. Then Indium content in In<sub>x</sub>Ga<sub>1-x</sub>N quantum dots can change the performance of laser diode (LD) [9] and indium (In) content can change InGaN crystal quality and optical properties [10]. However, the first principle study on the electronic structure and optical properties of the In<sub>x</sub>Ga<sub>1-x</sub>N alloy are rarely reported. In this paper, the electronic structure and optical properties of In<sub>x</sub>Ga<sub>1-x</sub>N alloy were discussed by firstprinciples calculations based on the density functional theory (DFT). Also the photoelectric properties of the In<sub>x</sub>Ga<sub>1-x</sub>N alloy with different Indium content were discussed in details, which provide an important theoretical basis for the research photoelectric devices and sensors.

# 2. THEORETICAL MODEL AND CALCULA-TION METHOD

The crystal model of InN and In<sub>x</sub>Ga<sub>1-x</sub>N on the calculation is hexagonal wurtzite structure like GaN crystal, whose bulk phase is part of P63mc space group, the symmetry is  $C_{6V}^4$  [11]. A part of the unicellular model of GaN is firstly created and optimized to the stable single-cell structure, and the  $2 \times 2 \times 2$  super cellular model containing 16 Ga atoms and 16 N atoms is constructed with a stable single cell model. In order to calculate and study electronic structure and optical performance of In<sub>x</sub>Ga<sub>1-x</sub>N in different concentration of In, a uniform distribution model of In atoms in GaN is selected under each x, and the  $2 \times 2 \times 2$ super-cell models with 50 % contents of In are shown in Fig. 1, where then N atoms are blue, Ga atoms are gray and In atoms are pink, and the lattice constants of InN super-cell model are a = 0.3523 nm, b = 0.3523 nm, c = 0.5688 nm,  $\gamma = 120^{\circ}, \alpha = \beta = 90^{\circ}, \text{ wherein } c/a = 1.614.$ 



**Fig. 1.** The unit cell of wurtzite GaN and super cell models of  $In_xGa_{1-x}N$ . In the figure, Blue: N atoms, Gray: Ga atoms and Pink: In atoms (in colour online)

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The unit cell of wurtzite GaN and super cell models of  $In_{0.5}Ga_{0.5}N$  are shown in Fig. 1, all In atoms are substitutional for Ga atoms in GaN and are distributed in the model as evenly as possible, which models are as similar as possible to alloy mode in principle.

In this paper, MS CASTEP module of software Materials-studio 8.0 is used for the theoretical calculation in order to predict the electronic structures and photoelectric properties of real  $In_xGa_{1-x}N$  materials. It is based on the plane-wave pseudo potential method from the DFT (Density Functional Theory) of ab initio quantum mechanics and GGA-PW91 function is used in the calculation [12]. Under the allowable situation of the hardware resources and the determinate convergence of system energy at the level of the quasi- complete fundamental wave. The k point selection of  $In_xGa_{1-x}N$  is  $4 \times 4 \times 2$ , the cutoff energy is selected to be 310 eV. The force convergence accuracy on each atom should be less than  $2.0 \times 10^{-5}$ eV/atom and internal stress convergence accuracy should be less than 0.1 GPa.

# 3. THE ANALYSIS OF CALCUATION RESULTS

# 3.1. Electrical structure analysis of In<sub>x</sub>Ga<sub>1-x</sub>N crystals

#### 3.1.1. Lattice constants

In this paper, we used the optimized GaN super cell model and replaced Ga atoms in GaN with In atoms. Then they were distributed evenly in the In<sub>x</sub>Ga<sub>1-x</sub>N model in proportion and the GGAPW91 was used to calculate. The calculation results show that the lattice constants of In<sub>x</sub>Ga<sub>1-x</sub>N crystals can change with the increase of x, as listed in Table 1. When x = 0 and x = 1, the computed data of the lattice constants are different from the experimental values, for example  $a_{GaN} = b_{GaN} = 3.189$ Å,  $c_{GaN} = 5.185$ Å [13],  $a_{InN} = b_{InN} = 3.548 \text{ Å}$ ,  $c_{InN} = 5.760 \text{ Å}$  [14]. The computed data of the lattice constants are slightly larger than experimental values which is caused by GGA. The difference of  $a_{GaN}$  is 1.25 % from the practical value, the one of  $c_{GaN}$  is 1.48 %, one of  $c_{GaN}(a_{GaN})^{-1}$  is 0.23 %, one of  $a_{InN}$  is 2.23 %, one of  $c_{InN}$  is 1.94 %, and one of  $c_{InN}(a_{InN})^{-1}$  is 0.276 %. The results are in the admitted error range since the calculation method is the same as literature [14]. From Table 1, when In replaces of Ga, the values of both a and c in In<sub>x</sub>Ga<sub>1-x</sub>N trend to increasing along with x, meanwhile the volume of cell also shows an increasing trend, which can abide by Vegard's Law. It is very easy to understand the radius of In<sup>3+</sup> of 0.08 nm is bigger than one of Ga<sup>3+</sup> of 0.62 Å.

Table 1. The lattice constants of  $In_xGa_{1-x}N$  (x = 0, 0.25, 0.5, 0.75, 1) crystals

	x = 0	x = 0.25	x = 0.5	x = 0.75	x = 1
a = b(Å)	3.229	3.334	3.449	3.529	3.627
c(Å)	5.262	5.408	5.527	5.709	5.872

#### 3.1.2. Energy band and electronic density of states

In the calculation of electrical properties of  $In_xGa_{1-x}N$  crystals, the band structures of  $In_xGa_{1-x}N$  with different x are calculated, which are similar to one of the  $In_{0.5}Ga_{0.5}N$  as

shown In<sub>8</sub>Ga<sub>8</sub>N<sub>16</sub> in Fig. 2. In<sub>0.5</sub>Ga<sub>0.5</sub>N are situated on the same position in k space that the top of conduction band and the vertex of valence band, which shows that the  $In_{0.5}Ga_{0.5}N$ crystal belongs to the direct band gap semiconductor, and the band-gap width is 0.539 eV. The values of optical band gap ( $E_g$ ) while x varies into 0, 0.25, 0.5, 0.75 and 1 are 1.621, 1.165, 0.539, 0.361 and 0.321 eV respectively. Compared with the experiment values (3.4 eV) of GaN and (0.70 eV) of InN, we plus the scissors operator in order to make up the gap (1.621 eV) into 3.4 eV, or 0.321 eV into 0.7 eV, so that the calculated  $E_g$  is more accurate. The 1.131 eV in Fig. 2 is a modified value from the calculated one (0.539 eV) of the In<sub>0.5</sub>Ga<sub>0.5</sub>N and a scissors difference of 0.592 eV [15]. The reason that the theoretically calculated value one is much less than the experimental one is what the exchange-correlation energy used in the GGA of MS software is an exchange-correlation functional primary approximation. Due to the adoption of GGA exchange function so that the band-gap width is undervalued. However, it cannot affect the analysis of the E<sub>g</sub> change trend of the similar structure crystals with different x under the same calculation conditions, and the data above shows that  $E_g$  can be reduced with the increase of x in  $In_xGa_{1-x}N$ . With the increasing of indium component, the bottom of the conduction band moves slightly towards the low energy direction, which is called a red shift phenomenon [16].

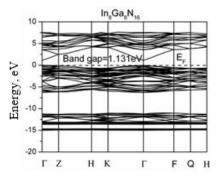


Fig. 2. Band structure of In<sub>0.5</sub>Ga<sub>0.5</sub>N

The density of states (DOS) of  $In_{0.5}Ga_{0.5}N$  is shown in Fig. 3 a. It follows that the electron energy bands include one conduction band of  $1.6 \sim 6 \text{ eV}$  and two valence bands in the left which are separately called as the lower valence band of  $-17 \text{ ev} \sim -11 \text{ eV}$  and the upper valence band of  $-7.5 \text{ eV} \sim 0 \text{ eV}$ . Fig. 3 b shows the partial density of states of different atoms, where s, p, d and f represent electronic sub-shells respectively. It shown that the lower valence band of  $In_{0.5}Ga_{0.5}N$  is resulted from Ga3d In 4d and N 2s. The conduction band consists of the 4s and 4p states of Ga atoms, 5s and 5p states of In atoms and 2s and 2p states of N atoms. The peak in -13 eV is generated by the Ga 3d state and the In 4d state, while the peak in -16eV is mostly provided by the N 2s.

Being compared to the electronic DOS of GaN, the relative positions of various peaks move to low energy are about 0.753 eV, which is due to that optical band gap narrows down. The intensity of the peaks in the conduction band doesn't change, and the intensity of the peaks in -11.5 eV and -6 eV falls down which results from In atoms. At the same time, the Fermi level moves slightly to the bottom of the conduction band, which indicates that the

electrical conductibility of the crystal enhances to some extent.

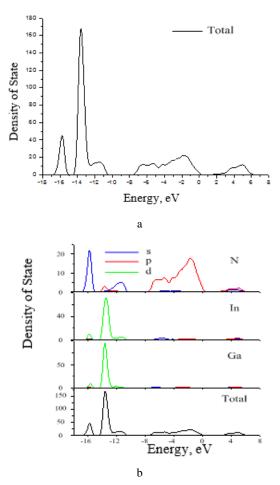


Fig. 3. Density of states of In<sub>0.5</sub>Ga<sub>0.5</sub>N: a – electronic density of states; b – partial density of states

# 3.2. The discuss of calculation characteristics of In<sub>x</sub>Ga<sub>1-x</sub>N crystals

While a light with wavelength  $\lambda$  and frequency  $\omega$ propagates in In<sub>x</sub>Ga<sub>1-x</sub>N crystal, the complex refractive index  $n^*(\omega)$  of the crystal is equal to the value that is  $n(\omega) + in_k(\omega)$ . The  $n(\omega)$  and  $n_k(\omega)$  are the real part and the imaginary part (namely extinction coefficient) of the complex refractive index In, respectively. The absorption coefficient ( $\alpha(\omega)$ ) of the crystal is in proportion to ( $n_k(\omega)$ ) and the optical frequency  $(\omega)$  seeing in Eq. 1. In consideration of that the complex dielectric constant ( $\varepsilon_1 + i\varepsilon_2$ ) of the crystal can generally represent the macroscopic optical response of the crystal and may make known the luminous mechanism of the electron transitions between energy levels of the crystal microcosmically. The  $\varepsilon_2$ ,  $\varepsilon_1$  can be deduced in accordance with the definition of a direct transition probability and Kramers-Kroning dispersion relation. So the  $\alpha(\omega)$ ,  $n(\omega)$  and  $n_k(\omega)$  optical parameters can be inferred from  $\varepsilon_2(\omega)$  and  $\varepsilon_1(\omega)$ , and the reflection coefficient  $(R(\omega))$  is only determined by  $n(\omega)$ ,  $n_k(\omega)$  and transmission coefficient  $(T(\omega))$  parameters. Wherein, Eq. 2 - Eq. 7 are derived from reference [17].

$$\alpha(\omega) = \frac{4\pi}{\lambda} n_k(\omega) = \frac{2}{c} n_k(\omega) \cdot \omega; \qquad (1)$$

$$\varepsilon_{2} = \frac{\pi e^{2}}{\varepsilon_{0} \mathrm{m}^{2} \omega^{2}} \sum_{\mathrm{V,C}} \int_{BZ} \frac{2dK}{(2\pi)^{3}} \left| a \cdot M_{CV}(K) \right|^{2} \delta[E_{c}(K) - E_{V}(K) - h\omega]$$
(2)

$$\varepsilon_{1} = 1 + \frac{2e}{\varepsilon_{0}m^{2}} \sum_{V,C} \int_{BZ} \frac{2dK}{(2\pi)^{3}} \frac{|a \cdot M_{VC}(K)|^{2}}{[E_{C}(K) - E_{V}(K)]/h} \cdot \frac{1}{[E_{C}(K) - E_{V}(K)]^{2}/h^{2} - \omega^{2}}$$
(3)

$$n(\omega) = \sqrt{\frac{\left(\varepsilon_1(\omega)\right)^2 + \left(\varepsilon_2(\omega)\right)^2 + \varepsilon_1(\omega)}{2}}; \qquad (4)$$

$$n_k(\omega) = \sqrt{\frac{(\varepsilon_1(\omega))^2 + (\varepsilon_2(\omega))^2 - \varepsilon_1(\omega)}{2}}; \qquad (5)$$

$$R(\omega) = \frac{(n(\omega) - 1)^2 + (n_k(\omega))^2}{(n(\omega) + 1)^2 + (n_k(\omega))^2};$$
(6)

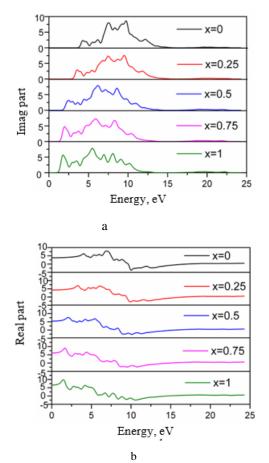
$$T(\omega) = 1 - \overline{\alpha(\omega)} - \overline{R(\omega)}.$$
<sup>(7)</sup>

Wherein, C and V mean the valence band and conduction band, BZ is the first Brillouin zone, respectively. *K* is the reciprocal lattice vector, *h* is the Planck constant,  $|aM_{VC}(k)|$  is the matrix elements of the momentum transition,  $E_c(k)$  is the conduction band of intrinsic energy levels and  $E_V(k)$  is valence band,  $\overline{\alpha(\omega)}$  or  $\overline{R(\omega)}$  is the value that  $\alpha(\omega)$  or  $R(\omega)$  is normalized to, respectively.

#### 3.2.2. Complex dielectric function

After calculation, the relation curves of the complex dielectric function including imaginary part ( $\varepsilon_2$ ) and real part ( $\varepsilon_1$ ) of In<sub>x</sub>Ga<sub>1-x</sub>N crystal with incident photon energy or angular frequency ( $\omega$ ) are shown in Fig. 4.

In Fig. 4 a, five curves from up to down represent GaN, In<sub>0.25</sub>Ga<sub>0.75</sub>N, In<sub>0.5</sub>Ga<sub>0.5</sub>N, In<sub>0.75</sub>Ga<sub>0.25</sub>N, InN, respectively. It can show that the number of peaks appearing in each curve is similar. The all peak positions shift to low energy direction in different extent with the increase of x. The result shows that the optical gap of In<sub>x</sub>Ga<sub>1-x</sub>N crystals constantly reduces and the lattice constant increases gradually with the increase of x. The peaks positions appearing in the  $\varepsilon_2$  curve are closely related to the electron transition between energy levels. For example,  $\varepsilon_2$  curve of GaN, in Table 2, when x = 0, the peak at 4.2 eV is the direct transition from valence band to conduction band of N 3p state. The peaks at 7.5 eV, 9.8 eV and 12.2 eV in  $\varepsilon_2$  curve of GaN are caused by the electron transitions between the valence bands whose electrons is the Ga 3d state and N 2s state of lower valence band or the N 2p state of upper valence band. In Fig. 4 b, the static dielectric constant value of the observation material is the longitudinal coordinate value of the 0 eV photon energy. The static dielectric constant is 3.97, 4.63, 5.59, 6.28 and 6.47 while x is 0, 0.25, 0.5, 0.75 and 1 respectively, which will be increased gradually with the increase of x component. With the increase of In component x, the static dielectric constant increases gradually. This is because the band gap value gradually decreases or narrows, electrons need only a small amount of energy can be excited from the top of the valence band transition to the top of the conduction band, it is easy to be polarized, so the value of the dielectric constant will gradually increase [18]. The peak positions appearing in  $\varepsilon_1$  curve are gradually moving towards the low energy state, which is consistent with the change trend of the imaginary part  $\varepsilon_2$  of the complex dielectric function.



**Fig. 4.** Relation curves of complex dielectric function of  $In_xGa_{1-x}N$  crystals and incident photon energy:  $a - \varepsilon_2$  in different x;  $b - \varepsilon_1$  in different x

**Table 2.** In the imaginary part of the complex dielectric function of  $In_xGa_{1-x}N$  (x = 0, 0.25, 0.5, 0.75, 1), there are five strong peaks

Unit, eV	1	2	3	4	5
GaN	4.2	7.5	9.8	12.2	19.6
In0.25Al0.75N	3.2	7.3	9.5	11.9	18.7
In <sub>0.5</sub> Al <sub>0.5</sub> N	2.5	6.7	8.9	10.8	18
In0.75Al0.25N	2.3	5.9	8.3	10.5	17.5
InN	2.1	5.5	7.7	10.1	17.0

### 3.2.2. Optical absorption and transmission

The optical absorption curves and the cut-off edge of absorption curves of  $In_xGa_{1-x}N$  (x = 0, 0.25, 0.5, 0.75, 1) are calculated theoretically are presented in Fig. 5. It can be found from the comparison of Fig. 5 a and Fig. 4 a that the peak positions are approach to the ones of the  $\varepsilon_2$  dielectric function while the In density has great difference. The absorption spectrum reaches the strongest peak at about 9.5 eV, which can be caused by the transitions of Ga 3d state and N 2p state shown in Fig. 3, consistent with reference [19]. The cut-off edge of absorption curves of  $In_xGa_{1x}N$  (x = 0, 0.25, 0.5, 0.75, 1) models from Fig. 5 b can be gotten as 364 nm, 460 nm, 835 nm, 1087 nm and 1402 nm, that is similar to the result of reference [20, 21], so it is show that the simulation method is feasible.

It is seen from Fig. 5 a that the absorption curves of  $In_xGa_{1-x}N$  gradually shift to long wave direction with the increase of x. It explains the absorption wavelength occurs "red shift" phenomenon to the infrared band, which results in presenting a narrow absorption band with the small intensity in long wavelength range, covering the visible to infrared wavelength range. So people can use the characteristics of  $In_xGa_{1-x}N$  materials to design infrared optoelectronic devices.

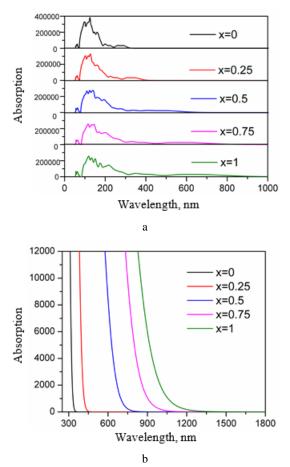


Fig. 5. The absorption spectrum and its cut-off edge of In<sub>x</sub>Ga<sub>1-x</sub>N: a-the absorption spectrum; b-cut off edge graph of absorption spectrum

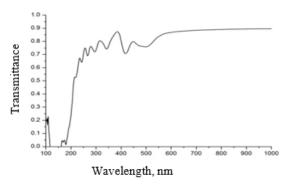


Fig. 6. Optical transmittance of intrinsic In0.5Ga0.5N crystal

The transmittance *T* can be calculated by using seven Formula above, and Fig. 6 shows one of the  $In_{0.5}Ga_{0.5}N$  with x = 0.5. We can find out that the transmittance change is irreguar before 560 nm, then transmittance gradually achieves smooth, the transmission rate decreases 88 % that

is smaller than 93 % of intrinsic GaN. The wavelength range of absorption and transmission of  $In_xGa_{1-x}N$  includes sunlight, infrared light and ultraviolet light. The stable transmission wavelength is longer, consistent with the changing trend of the experimental data in reference [22], it can be applied to a wide wavelength solar cell, a photoelectric device, and a sensor.

# 4. CONCLUSIONS

In this paper, we first constructed the supercell GaN crystal and calculated the optimized photoelectric characteristics, then build the super-cell In<sub>x</sub>Ga<sub>1-x</sub>N with the different density of In, then the electrical structure and photoelectric characteristics were calculated. The results found, with the increase of In concentration, both the values of a and c of In<sub>x</sub>Ga<sub>1-x</sub>N enlarge, In<sub>x</sub>Ga<sub>1-x</sub>N is direct gap semiconductor, and optical band gap (Eg) decreases, and the conductivity becomes strong. From the calculation results of the complex dielectric function, we know that the peak positions in the imaginary part shift to low energy direction, and the static dielectric function of the real part is increased. Due to the increase of In concentration, the absorption spectrum shifted to low energy region and this cut-off edge shifts to the long wavelength direction, the transmittance change worse. In brief, it can adjust that photoelectric property by changing the ratio of In atom to Ga atom in the In<sub>x</sub>Ga<sub>1-x</sub>N semiconductor. alloy The conductive performance of In<sub>x</sub>Ga<sub>1-x</sub>N enhances with the increase of In concentration, and the absorption spectrum shows "red shift" phenomenon. This experiment meets the development trend of InN-based materials and can be advantageous to the development application in optoelectronic device and sensor fields.

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